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# Bonding interactions in $Ag^+(O_2)_n$ and $Ag_2^+(O_2)_n$ clusters: experiment and theory

Manuel J. Manard, Paul R. Kemper, Michael T. Bowers\*

Department of Chemistry & Biochemistry, University of California, Santa Barbara, CA 93106, USA

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Dedicated to Prof. Helmut Schwarz on the occasion of his 60th birthday.

#### Abstract

Equilibrium methods were used to measure binding energies and entropies for the attachment of up to four  $O_2$  ligands to ground-state  $Ag^+(^1S, 4d^{10})$  and for the attachment of up to three  $O_2$  ligands to ground-state  $Ag_2^+(^2\Sigma_g, 4d^{20} \sigma(5s)^1)$ . Bond dissociation energies (BDEs) of the first three  $O_2$  ligands from  $Ag^+(O_2)_n$  are 6.9, 7.4, and 5.5 kcal/mol for n=1–3, respectively, with the BDE of the fourth ligand estimated to be 4.8 kcal/mol. BDEs of the first and second  $O_2$  ligands from  $Ag_2^+(O_2)_n$  are 4.5 and 4.2 kcal/mol, respectively, with the BDE of the third ligand estimated to be 3.5 kcal/mol. All of the observed attachments of  $O_2$  ligands to both the monomer and dimer Ag core ions were within the first solvation shell. Theoretical calculations at the DFT-B3LYP level were done on all of the observed  $Ag^+$  and  $Ag_2^+$  clusters in order to determine the vibrational frequencies and geometries and to examine the origin of the bonding and its variation with core ion coordination. Comparisons are made with the  $Cu^+(H_2)_n$  and  $Cu_2^+(H_2)_n$  systems.

Keywords: Bonding interactions;  $Ag^+(O_2)_n$  cluster;  $Ag_2^+(O_2)_n$  cluster

### 1. Introduction

From biological systems to industrial processes, transition metals have proven to be essential components of a vast array of catalytic reactions. Despite their widespread usage, many of the details of how transition metals aid these reactions remain essentially unknown. However, over the past 15 years, experiments conducted on gas phase transition metal ion clusters have shed new light on this subject [1–19]. These experiments have broadened our understanding

of the nature of transition metal ion bonding from a simple electrostatic view to an awareness of the complex covalent factors that are involved. Many of these experiments have examined the binding between oxidized transition metal core ions with small, uninserted ligands. This was first shown to be possible by the experiments of Kubas et al. [1], where uninserted  $H_2$  molecules were bound to a transition metal center. In the time that has followed, systematic experiments have examined the properties of numerous gas phase metal ion  $M^+ - X_n$  [2–19] clusters. Relatively simple systems with  $X = H_2$  [2–12], CO [13–18], and methane [3,19] have been examined, along with a variety of other ligands [20,21]. The influence of the electronic structure of the metal ion on both the binding

fax: +1-805-893-8703.

E-mail address: bowers@chem.ucsb.edu (M.T. Bowers).

<sup>\*</sup> Corresponding author. Tel.: +1-805-893-2893;

energies and structures of these clusters clearly show the presence of covalent forces in the bonding. The large difference in  $M^+ - X_n$  bond energies between the truly inert alkali ions and the transition metals reinforces this observation [22]. Additionally, the relatively small size of these clusters makes them well suited for modeling with high-level ab initio calculations. These calculations have proven necessary to gain a complete understanding of both the structures and the underlying bonding processes present in these systems [20]. The ability to examine these relatively small transition metal clusters in great detail makes them excellent prototype systems for studying the elementary steps of their catalytic processes.

Recently, there has been an increased interest in the bonding interactions of Au and Ag clusters with O<sub>2</sub>. This is due to the recent discovery that small Au clusters are good oxidation catalysts [23]. Although theoretical investigations into the binding characteristics of O2 with Ag and Au clusters, both ionic and neutral, have been conducted in order to determine binding energies, molecular geometries, and other properties [24,25], and some experiments have also been performed to measure binding energies of negative Au clusters with O<sub>2</sub> ligands [26–29], detailed information about these newly discovered catalytic properties of Ag and Au is not yet available. To help elucidate the origin of their catalytic properties, we have initiated a broad-based effort at University of California, Santa Barbara to investigate these properties, both for clusters on metal oxide surfaces and in the gas phase. Our initial studies are reported here where  $Ag^+(O_2)_n$  and  $Ag_2^+(O_2)_n$  clusters were examined using temperature-dependent equilibrium measurements as well as ab initio calculations. Of particular interest is the nature of the interaction of these Ag clusters with O<sub>2</sub> and how these interactions compare with the analogous  $Cu^+(H_2)_n$  [11] and  $Cu_2^+(H_2)_n$  [12] clusters reported earlier. Although the ligands in the Cu and Ag studies differ, the similarities in the valence electronic structures of  $Ag^{+}(4d^{10})$  and  $Cu^{+}(3d^{10})$ , and  $Ag_{2}^{+}(4d^{20} \sigma(5s)^{1})$ and  $Cu_2^+(3d^{20} \sigma(5s)^1)$ , should prove interesting as a point of comparison. We present here a combined experimental and theoretical study of  $Ag^+(O_2)_n$  and  $Ag_2^+(O_2)_n$ .

## 2. Experimental

A description of the instrument and experimental details has been given previously [5,7,30], and only a brief description will be given here. The Ag+ and Ag<sub>2</sub><sup>+</sup> ions are generated from a translating/rotating silver rod with a pulsed laser vaporization ion source using an Ar bath gas. The preferred isotope (either  $^{107}Ag^+$  or  $^{109}Ag^+$  for the monomer or  $^{214}Ag_2^+$ ,  $^{216}\text{Ag}_2^+$  or  $^{218}\text{Ag}_2^+$  for the dimer) is then mass selected by a quadrupole mass filter and injected into a 4-cm long drift/reaction cell. The cell is typically filled with 1-4 Torr of O2 gas. Equilibria are quickly established as the various  $Ag^+(O_2)_n$  and  $Ag_2^+(O_2)_n$ clusters are drawn through the cell under the influence of a small electric field. The electric field is small enough so that the thermal energy of the ions is not significantly perturbed. The clusters exiting the cell are then mass selected by a second quadrupole and detected. Peak intensities are recorded and integrated and these values, along with the pressure of  $O_2(P_{O_2})$ in Torr, are used to determine an equilibrium constant  $(K_{\rm p}^{\circ})$  for the reaction from Eq. (1).

$$K_{\rm p}^{\circ} = \frac{[{\rm Ag_{1,2}}^{+}({\rm O_2})_n]}{[{\rm Ag_{1,2}}({\rm O_2})_{n-1}]} \times \frac{760}{P_{\rm O_2}}$$
 (1)

The equilibrium constant can then be used to calculate the standard Gibbs free energy of the reaction,

$$\Delta G_T^{\circ} = -RT \ln[K_{\mathfrak{p}}^{\circ}] \tag{2}$$

and the values obtained for  $\Delta G_T^{\circ}$  plotted vs. the temperature, to obtain  $\Delta S_T^{\circ}$  and  $\Delta H_T^{\circ}$  from Eq. (3)

$$\Delta G_T^{\circ} = \Delta H_T^{\circ} - T \, \Delta S_T^{\circ} \tag{3}$$

The resulting plots are linear over the experimental temperature range and a least squared fitting procedure is used to obtain slopes equal to the association entropy  $(\Delta S_T^{\circ})$  of the reaction and intercepts equal to the binding energy  $(\Delta H_T^{\circ})$  of the molecule. The reported uncertainty in these values is a measure of variance in

the data from the fit.  $\Delta H_0^\circ$  is then determined by fitting and extrapolating the data to 0 K using statistical thermodynamics. The necessary vibrational frequencies and rotational constants are taken from density functional theory (DFT) [31] calculations (see next section). In all cases, vibrational frequencies are varied over a wide range, and the effect on  $\Delta H_0^\circ$  is included in the error limits. It should be stressed that uncertainties in these parameters have little effect on the final values of  $\Delta H_0^\circ$ . For a thorough discussion of this fitting procedure and an estimation of the errors involved, see Refs. [2] and [5]. The bond dissociation energy (BDE) is equal to  $-\Delta H_0^\circ$ .

## 3. Theory

The product ions discussed here were all examined theoretically to determine the molecular parameters needed to analyze the experimental data and to identify factors important in the bonding. Calculations were carried out at the DFT level using the B3LYP hybrid functional [32,33], using the Gaussian 98 package [34]. For all of the calculations performed in this work, oxygen was described using the standard 6-311+G\* basis set [35]. The basis set for silver is a (5s6p4d)/[3s3p2d] contraction of the Hay-Wadt (n+1) effective core potential (ECP) valence double zeta basis proposed by Hay and Wadt [36]. Here, the outermost core orbitals are not replaced by the ECP, but are instead treated equally with the valence orbitals. This allows for increased accuracy in the calculations without a substantial increase in computation time. The ECP for silver incorporates the Darwin and mass-velocity relativistic effects into the potential.

Geometry optimizations of  $Ag^+(O_2)_n$  and  $Ag_2^+(O_2)_n$  clusters were performed over a wide range of geometries in order to determine a true global minimum. All confirmed minima consist of largely unperturbed  $O_2$  ligands bound to a transition metal core ion. Vibrational frequencies were calculated for all minima. All reported vibrational frequencies are unscaled.

#### 4. Results and discussion

A summary of the experimental enthalpies and entropies as well as theoretical binding energies for the reaction  $Ag^+(O_2)_{n-1} + O_2 \rightleftharpoons Ag^+(O_2)_n$  is given in Table 1. The corresponding calculated vibrational frequencies are listed in Table 2. Experimental enthalpies, entropies, and theoretical binding energies for the reaction  $Ag_2^+(O_2)_{n-1} + O_2 \rightleftharpoons Ag_2^+(O_2)_n$  are given in Table 3 and the corresponding calculated vibrational frequencies are listed in Table 4. All of the cluster ions discussed here consist either of an intact  $Ag^+$  or  $Ag_2^+$  core ion surrounded by largely unperturbed  $O_2$  ligands. No evidence of insertion to form a dioxide was found.

# 5. $Ag^+(O_2)_n$ clusters

5.1. 
$$Ag^+(O_2)$$

The experimental  $\Delta H_T^\circ$  and  $\Delta S_T^\circ$  values for dissociation of  $\mathrm{Ag^+}(\mathrm{O_2})$  are  $-7.1\,\mathrm{kcal/mol}$  and  $-15.0\,\mathrm{cal/}$  (mol K), respectively (Table 1). Fig. 1 shows both the experimental free energy and that calculated from statistical mechanics using theoretically determined vibrational frequencies (Table 2) and rotational constants. The resulting experimental BDE  $(-\Delta H_0^\circ)$  of  $\mathrm{Ag^+}(\mathrm{O_2})$  is 6.9 kcal/mol, in good agreement with the calculated (DFT) binding energy  $(D_0)$  of 6.30 kcal/mol. The first  $\mathrm{O_2}$  ligand adds in a bent triatomic conformation to  $\mathrm{Ag^+}$  (Fig. 2). The calculated  $\mathrm{Ag^+}$ – $\mathrm{O_2}$  bond distance is 2.466 Å with an associated O–O bond length of 1.204 Å, shorter than the theoretical O–O bond distance of 1.206 Å calculated for free  $\mathrm{O_2}$ . The  $\mathrm{Ag}$ –O–O angle of  $\mathrm{Ag^+}(\mathrm{O_2})$  is 137.5°.

<sup>&</sup>lt;sup>1</sup> Basis sets were obtained from the Extensible Computational Chemistry Environment Basis Set Database, Version 10/29/02, as developed and distributed by the Molecular Science Computing Facility, Environmental and Molecular Sciences Laboratory which is part of the Pacific Northwest Laboratory, P.O. Box 999, Richland, Washington 99352, USA, and funded by the U.S. Department of Energy. The Pacific Northwest Laboratory is a multi-program laboratory operated by Battelle Memorial Institute for the U.S. Department of Energy under contract DE-AC06-76RLO 1830. Contact David Feller or Karen Schuchardt for further information.

Table 1 Data summary for  $Ag^+(O_2)_{n-1} + O_2 \overline{+} Ag^+(O_2)_n$ 

Experiment					Theory	
n	$-\Delta H_T^{\circ \ \mathrm{a}}$	$-\Delta S_T^{\circ   \mathrm{b}}$	$-\Delta H_0^{\circ c}$	$T^{\mathrm{d}}$	$\overline{{D_{\mathrm{e}}}^{\mathrm{a}}}$	$D_{\mathrm{o}}^{\mathrm{a}}$
1	$7.1 \pm 0.2$	15.0 ± 1	$6.9 \pm 0.3$	310 ± 75	6.66	6.30
2	$7.6 \pm 0.2$	$21.4 \pm 1$	$7.4 \pm 0.3$	$220 \pm 40$	7.11	6.47
3	$5.7 \pm 0.2$	$19.3 \pm 2$	$5.5 \pm 0.3$	$160 \pm 20$	4.58	4.24
4			4.8 <sup>e</sup>	140	4.16	3.91

<sup>&</sup>lt;sup>a</sup> In units of kcal/mol.

Table 2 Theoretical vibrational frequencies for  $Ag^+(O_2)_n$  clusters<sup>a,b</sup>

	O–O stretch	Ag <sup>+</sup> -O <sub>2</sub> symmetric stretch	Ag <sup>+</sup> -O <sub>2</sub> asymmetric stretch	O <sub>2</sub> -Ag <sup>+</sup> -O <sub>2</sub> bends and torsions
$Ag^+(O_2)$	1622	177		87
$Ag^{+}(O_{2})_{2}$	1622(2)	175	204	25°, 60, 62, 94, 111
$Ag^{+}(O_{2})_{3}$	1625(2), 1626	154	159, 169	17°, 23°, 28°, 31, 34, 52, 82, 85, 90
$\begin{array}{c} Ag^+(O_2)_4 \\ O_2 \end{array}$	1626, 1627(3) 1633	144	142, 143, 150	8°, 13, 15°, 17°, 19, 25°, 33, 39, 40, 73(2), 79, 82

<sup>&</sup>lt;sup>a</sup> Harmonic vibrational frequencies for the different  $Ag^+(O_2)_n$  clusters as obtained by analytical differentiation of the SCF energy at SCF geometry.

The bonding characteristics of  $Ag^+(O_2)$  set trends that are closely followed in the larger  $Ag^+(O_2)_n$  clusters. Although the bond strengths in these clusters are relatively weak, never exceeding 7.4 kcal/mol, there is evidence that the bonding interaction between  $Ag^+$  and  $O_2$  is covalent rather than purely electrostatic. Cal-

culations show that about 0.1 electron is donated to  $Ag^+$  in  $Ag^+(O_2)$ . Upon bonding with  $Ag^+$ , a partial negative charge is found on the O atom closest to the transition metal ion, while a partial positive charge is found on the other O atom. This positive charge is slightly greater in magnitude than that of the negative

Table 3 Data summary for  $Ag_2^+(O_2)_{n-1} + O_2 \rightleftarrows Ag_2^+(O_2)_n$ 

Experiment					Theory	
$\overline{n}$	$-\Delta H_T^{\circ a}$	$-\Delta S_T^{\circ b}$	$-\Delta H_0^{\circ c}$	$T^{\mathrm{d}}$	$\overline{D_{\mathrm{e}}^{\mathrm{a}}}$	$D_0^{a}$
1	$4.9 \pm 0.4$	16.5 ± 2	$4.5 \pm 0.5$	175 ± 25	4.20	3.78
2	$4.5 \pm 0.3$	$16.0 \pm 3$	$4.2 \pm 0.4$	$135 \pm 15$	3.56	3.16
3			3.5 <sup>e</sup>	120	2.03	1.76

a In units of kcal/mol.

<sup>&</sup>lt;sup>b</sup> In units of cal/(mol K).

c Value from fitting data with theoretical vibrational frequencies, rotational constants and geometries, in units of kcal/mol.

<sup>&</sup>lt;sup>d</sup> In Kelvin, ± refers to the experimental temperature range not uncertainty.

<sup>&</sup>lt;sup>e</sup> Estimate, assuming the same  $\Delta S_T^{\circ}$  as n=3 (see text).

<sup>&</sup>lt;sup>b</sup> All numbers in cm<sup>-1</sup>.

<sup>&</sup>lt;sup>c</sup> Free rotations.

<sup>&</sup>lt;sup>b</sup> In units of cal/(mol K).

<sup>&</sup>lt;sup>c</sup> Value from fitting data with theoretical vibrational frequencies, rotational constants and geometries, in units of kcal/mol.

 $<sup>^{</sup>m d}$  In Kelvin,  $\pm$  refers to the experimental temperature range not uncertainty.

<sup>&</sup>lt;sup>e</sup> Estimate, assuming the same  $\Delta S_T^{\circ}$  as n=2 (see text).

Table 4 Theoretical vibrational frequencies for  $Ag_2^+(O_2)_n$  clusters<sup>a,b</sup>

	Ag-Ag symmetric stretch	O-O stretch	Ag <sub>2</sub> <sup>+</sup> -O <sub>2</sub> symmetric stretch	Ag <sub>2</sub> <sup>+</sup> -O <sub>2</sub> asymmetric stretch	$O_2$ - $Ag_2$ <sup>+</sup> - $O_2$ bends and torsions
$Ag_2^+(O_2)$	116	1629	152		30, 53, 73
$Ag_2^+(O_2)_2$	109	1630(2)	152	124	20 <sup>d</sup> , 29, 30, 50, 55, 73, 66
$Ag_2^+(O_2)_3$	107	1629, 1630°, 1631°	142	98, 113	15, 16 <sup>d</sup> , 24(2) <sup>d</sup> , 27, 33, 35, 46, 49, 59, 65
$Ag_2^+$	124				
$O_2$		1633			

<sup>&</sup>lt;sup>a</sup> Harmonic vibrational frequencies for the different  $Ag_2^+(O_2)_n$  clusters as obtained by analytical differentiation of the SCF energy at SCF geometry.

charge on the O atom directly bonded to Ag<sup>+</sup>. In other words, the positive charge of Ag<sup>+</sup> induces a dipole moment on the O<sub>2</sub> ligand in which electron density is drawn toward Ag<sup>+</sup>. The reduced positive charge of Ag<sup>+</sup> along with the net partial positive charge of the O<sub>2</sub> ligand indicates that electron density is indeed shared between Ag<sup>+</sup> and O<sub>2</sub>, which is, by definition, a covalent bond. The charge distribution is given in Fig. 2.

The  $\mathrm{Ag}^+$  ion has a  $4d^{10}$   $5\mathrm{s}^0$  valence configuration, which suggests that the majority of charge donation to  $\mathrm{Ag}^+$  is to the unoccupied 5s orbital since the 4d orbitals are fully occupied and the 5p orbitals lie much higher in energy than the 5s orbital. This would be quite similar to the bonding interactions of  $\mathrm{Cu}^+(\mathrm{H}_2)$  [11], where most of the charge transfer from the  $\mathrm{H}_2$  ligand is to the unoccupied 4s orbital of  $\mathrm{Cu}^+$ . The ground-state of  $\mathrm{O}_2$  is a triplet, with two unpaired

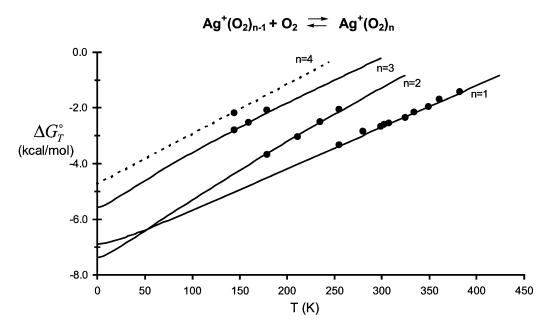


Fig. 1. Plot of experimental  $\Delta G_T^{\circ}$  vs. temperature for the association reactions  $Ag^+(O_2)_{n-1} + O_2 \neq Ag^+(O_2)_n$ . Lines are statistical mechanical fits to the data, which yield values of  $\Delta H_0^{\circ}$  at T = 0 K.

<sup>&</sup>lt;sup>b</sup> All number in cm<sup>-1</sup>.

<sup>&</sup>lt;sup>c</sup> Angled O<sub>2</sub> pair.

d Free rotations.

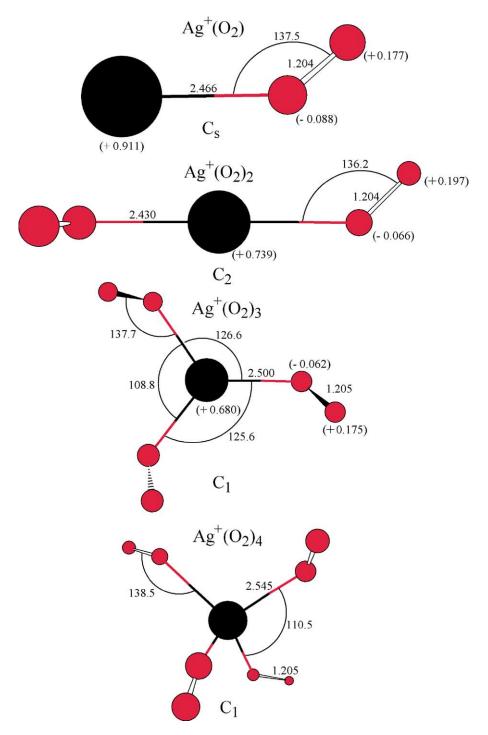


Fig. 2. Theoretical geometries of the  $Ag^+(O_2)_n$  clusters calculated at the DFT B3-LYP level. All distances are in angstroms and all angles are in degrees. Partial atomic charges are shown in parentheses. The z-axis is taken as the  $Ag^+-O_2$  bonding axis.

electrons in degenerate  $\pi^*(2p_x, 2p_y)$  antibonding orbitals. This suggests that donation to Ag<sup>+</sup> should originate from one of the  $\pi^*(2p_{x,y})$  orbitals of O<sub>2</sub>. NBO population analysis [37] supports this hypothesis. Calculations show that the dominant bond interaction is indeed donation from  $\pi^*(2p_{x,y})$  orbital of  $O_2$  to the 5s orbital of Ag<sup>+</sup>. This is supported by the relatively weak binding energy of the cluster. Since it is well known that O<sub>2</sub> is a better electron acceptor than donor, electron donation from the  $\pi^*(2p_{x,y})$  orbital of  $O_2$  is no doubt an unfavorable process which gives rise to the overall weak bonding interaction of  $Ag^+(O_2)$ . NBO populations also show that the majority of the electron density present in the 5s orbital of  $Ag^+$  has  $\alpha$  spin. This would be expected if donation was from a singly occupied  $\pi^*(2p_{x,y})$  orbital. The calculations also indicate that some hybridization between the  $4d_{x^2-y^2}$  and 5s orbitals of Ag<sup>+</sup> occurs in order to reduce on-axis Pauli repulsion. This is a minor effect, however.

The suggested bonding scheme of  $Ag^+(O_2)$  is supported by the molecular geometry of the cluster. The 137.5° bond angle of  $Ag^+(O_2)$  indicates that electron donation must originate from the  $\pi^*(2p_{x,y})$  orbitals of  $O_2$ . Also, the calculated O–O bond distance of  $Ag^+(O_2)$  is slightly reduced compared to that of free  $O_2$  (1.2043 Å as compared to 1.2058 Å, respectively). This is expected since loss of repulsive antibonding electron density should decrease the O–O bond distance in the bound  $O_2$  ligand.

A secondary bonding interaction is also present in the cluster. Specifically, electron density is polarized into the  $\sigma^*(2p_z)$  orbital of  $O_2$ . The NBO calculation shows increased electron density in the  $2p_z$  orbitals of bound  $O_2$  compared to free  $O_2$ . Given that the  $\sigma(2p_z)$  orbital of  $O_2$  is fully occupied, the increased electron density in these orbitals must be in the  $\sigma^*(2p_z)$  orbital. The electron density present in the  $\sigma^*(2p_z)$  orbital of  $O_2$  experiences an attractive electrostatic force to  $Ag^+$ , which influences the geometry of the cluster. This can be observed by noting the fluctuations in the  $Ag^+-O-O$  bond angle in  $Ag^+(O_2)_n$  clusters where the  $5s/\pi^*(2p_{x,y})$  interaction is relatively strong compared to those where the interaction is weak. A stronger  $5s/\pi^*(2p_{x,y})$  interaction gives rise to bond angles

nearer 135°. From electron density contour plots of the  $\pi^*$  orbital of O<sub>2</sub>, this is what would be expected from a "pure"  $\pi^*(2p_{x,y})$  interaction [38]. As the  $5s/\pi^*(2p_{x,y})$ interaction weakens, Ag<sup>+</sup>-O<sub>2</sub> bond distances increase and Ag<sup>+</sup>-O-O bond angles increase. The latter event cannot be attributed to loss of  $\pi^*(2p_{x,y})$  donation alone. Instead, it is a combination of decreased  $\pi^*(2p_{x,y})$  donation coupled with an electrostatic attraction between Ag+ and the electron density polarized into the  $\sigma^*(2p_z)$  orbital of  $O_2$ . This electrostatic interaction causes Ag<sup>+</sup>–O–O bond angles to "open" as covalent  $\pi^*(2p_{x,y})$  interactions diminish. This interaction is minor in comparison to the  $\pi^*(2p_{x,y})$  donation. The NBO calculation shows that the amount of electron density in the  $\sigma^*(2p_z)$  orbital of  $O_2$  is essentially the same for all of the clusters that were examined here in both the Ag<sup>+</sup> and Ag<sub>2</sub><sup>+</sup> systems. This lack of change in electron density in the  $\sigma^*(2p_7)$  orbital for the larger clusters suggests that the interaction between the  $\sigma^*(2p_z)$  on  $O_2$  and the  $Ag^+$  ion is purely electrostatic and that the electron density in the  $\sigma^*(2p_z)$  orbital is not due to back donation from 4d orbitals on Ag<sup>+</sup>.

# 5.2. $Ag^+(O_2)_2$

The second O<sub>2</sub> ligand adds opposite the first as shown in Fig. 2 (C<sub>2</sub> symmetry). The experimental  $\Delta H_T^{\circ}$  and  $\Delta S_T^{\circ}$  values for loss of O<sub>2</sub> from Ag<sup>+</sup>(O<sub>2</sub>)<sub>2</sub> are  $-7.6 \,\text{kcal/mol}$  and  $-21.4 \,\text{cal/(mol K)}$ , respectively. The BDE of Ag<sup>+</sup>(O<sub>2</sub>)<sub>2</sub> was determined by fitting experimental and theoretical  $\Delta G_T^{\circ}$  vs. temperature curves and found to be 7.4 kcal/mol, up from 6.9 kcal/mol in the first cluster. The calculated (DFT) binding energy  $(D_0)$  for the second cluster is 6.47 kcal/mol, somewhat larger than the 6.30 kcal/mol value calculated for the first O2 ligand. The theoretical vibrational frequencies for  $Ag^+(O_2)_2$  are given in Table 2. The calculated Ag<sup>+</sup>-O<sub>2</sub> bond distances are 2.430 Å with associated O-O bond distances of 1.204 Å. The angle produced by an O<sub>2</sub> ligand and Ag<sup>+</sup> is 136.2°. Two alternative *cis*- and *trans*-planar conformations for Ag<sup>+</sup>(O<sub>2</sub>)<sub>2</sub> were found to have theoretical binding energies that are essentially degenerate with the C<sub>2</sub> conformation, differing from one another by only a few hundredths of kcal/mol. A transition state structure was then calculated in which one  $O_2$  ligand was rotated approximately  $45^\circ$  out of plane in order to determine the rotational barrier between the  $Ag^+(O_2)_2$  structures. The rotation barrier was found to approximately 0.1 kcal/mol. This approximate barrier height is well below the thermal energy available, indicating essentially free internal rotation in the system. Such free rotations are not uncommon and have been observed in other transition metal systems [12].

The bonding interactions in  $Ag^+(O_2)_2$  are fundamentally the same as those in  $Ag^+(O_2)$ , with  $O_2$  $\pi^*(2p_{x,y})$  donation to the 5s orbital of Ag<sup>+</sup> and a charge-induced dipole moment causing electron density of the  $O_2$  ligands to be polarized toward  $Ag^+$ . This can be seen by the partial negative charges on those O atoms of both O<sub>2</sub> ligands that are directly bonded to Ag<sup>+</sup>, and by the net loss of positive charge on Ag<sup>+</sup>. As with the first cluster, the electron density polarized into the  $\sigma^*(2p_z)$  orbitals of both  $O_2$  ligands plays a minor role in the bonding of Ag<sup>+</sup>(O<sub>2</sub>)<sub>2</sub>, via an electrostatic attraction to the Ag+ core ion. NBO population analysis shows that the populations of the  $\sigma^*(2p_z)$  orbitals of the O<sub>2</sub> ligands are essentially the same and are similar to that of the  $\sigma^*(2p_z)$  orbital of the  $O_2$  ligand of  $Ag^+(O_2)$ , providing support for the argument that this interaction is purely electrostatic.

The BDE of the second  $O_2$  ligand in  $Ag^+(O_2)_2$  is slightly larger than that of the first cluster. This effect is found for most other transition metal ions binding simple ligands, including the  $Cu^+(H_2)_{1,2}$  system. The effect arises from the hybridization of occupied d orbitals with the unoccupied s orbital that occurs when the first ligand binds. This hybridization reduces on-axis Pauli repulsion and is necessarily symmetric. When the second ligand binds, the cost of the hybridization has been paid by the first ligand, producing a larger BDE for the second ligand. In the present case, calculations show that in  $Ag^+(O_2)$  and  $Ag^+(O_2)_2$  a small amount of electron density is removed from the  $4d_{x^2-y^2}$  orbital and promoted into the 5s orbital of Ag<sup>+</sup>. The price of this hybridization is paid by the first O<sub>2</sub> ligand, giving rise to the slightly larger second cluster BDE.

The effect of a larger BDE can be seen in the cluster geometry of  $Ag^+(O_2)_2$ . The  $Ag^+-O_2$  bond lengths and angles of  $Ag^+(O_2)_2$  are slightly reduced relative to the analogous features in  $Ag^+(O_2)$ , suggesting a stronger  $\pi^*(2p_{x,y})/5s$  interaction. The O–O bond lengths of  $Ag^+(O_2)_2$  remain largely unchanged from those of  $Ag^+(O_2)$  however, indicating that the increase in the interaction is small. The larger value of  $\Delta S_T^\circ$  found in the second  $O_2$  association reaction (relative to the first), is mostly due to the loss of two rotational modes that occurs when  $Ag^+(O_2)$  reacts with  $O_2$  to form  $Ag^+(O_2)_2$ . When the atomic ion  $Ag^+$  reacts with  $O_2$  to form  $Ag^+(O_2)_2$ , rotational entropy increases giving a less negative  $\Delta S_T^\circ$  for the first association.

# 5.3. $Ag^+(O_2)_3$ and $Ag^+(O_2)_4$

Equilibrium for the Ag<sup>+</sup>(O<sub>2</sub>)<sub>3</sub> cluster could only be observed over a very limited temperature range (140–180 K). The experimental  $\Delta H_T^{\circ}$ and  $\Delta S_T^{\circ}$  values for Ag<sup>+</sup>(O<sub>2</sub>)<sub>3</sub> are -5.7 kcal/mol and -19.3 cal/(mol K), respectively. The BDE of Ag<sup>+</sup>(O<sub>2</sub>)<sub>3</sub> was determined by the usual fitting of experimental  $\Delta G_T^{\circ}$  vs. T plots and found to be 5.5 kcal/mol. The calculated (DFT) binding energy  $(D_0)$  of Ag<sup>+</sup> $(O_2)_3$  is 4.24 kcal/mol, again in reasonable agreement with experiment. It is of interest to note that theory predicts the observed reduction in BDE between the second and third clusters of approximately 2 kcal/mol. Theoretical vibration frequencies for  $Ag^+(O_2)_3$  are listed in Table 2. The calculated molecular geometry of  $Ag^+(O_2)_3$  is shown in Fig. 2. The calculated Ag<sup>+</sup>-O<sub>2</sub> bond distances are 2.500 Å with an associated O-O bond distance of 1.205 Å. The  $Ag^+$ –O–O bond angles of  $Ag^+$ (O<sub>2</sub>)<sub>3</sub> are approximately 137.7°. The inner O atoms (those directly bound to Ag<sup>+</sup>) and Ag<sup>+</sup> lie in the same plane. The outer O atoms are rotated a few degrees out from this plane, giving rise to a cluster geometry that is

The bonding of  $Ag^+(O_2)_3$  is similar to that seen in previous clusters with donation to the 5s orbital of  $Ag^+$  from the  $\pi^*(2p_{x,y})$  orbitals of the  $O_2$  ligands as the primary bonding interaction. Again, an electrostatic

interaction between the  $\sigma^*(2p_z)$  orbitals of the  $O_2$  ligands and  $Ag^+$  plays a minor role in the bonding of the cluster. Charge-induced dipole moments are once again found on the  $O_2$  ligands, causing electron density to be polarized toward the  $Ag^+$  and eventually, transferred into unoccupied 5s orbital of the transition metal core ion.

The reduced BDE of  $Ag^+(O_2)_3$  can be attributed to a reduction in the covalent interaction of the cluster. NBO population analysis indicates similar amounts of electron density in the 5s orbital of  $Ag^+$  for both the  $Ag^+(O_2)_2$  and  $Ag^+(O_2)_3$  clusters. Since the three  $O_2$  ligands of  $Ag^+(O_2)_3$  are donating similar amounts of  $\pi^*(2p_{x,y})$  electron density as the two  $O_2$  ligands of  $Ag^+(O_2)_2$ , it is clear that the average covalent bonding in the third cluster is weaker than that in the second. This reduced covalent interaction is also indicated by the increased  $Ag^+-O_2$  bond distances in the third cluster.

Data for Ag<sup>+</sup>(O<sub>2</sub>)<sub>4</sub> was only taken at 140 K. A BDE of 4.8 kcal/mol for Ag<sup>+</sup>(O<sub>2</sub>)<sub>4</sub> was estimated by assuming an association entropy equal to that of the third cluster. The DFT optimized structure for

 $Ag^+(O_2)_4$  is shown in Fig. 2. The theoretical binding energy  $(D_0)$  for  $Ag^+(O_2)_4$  is 3.9 kcal/mol slightly lower than the 4.2 kcal/mol calculated for the third association. The calculated geometry of the fourth cluster is quasi-tetrahedral and shows evidence of a further reduction of covalent interaction in that the  $Ag^+-O_2$  bond distances increase from 2.500 to 2.545 Å as the fourth  $O_2$  ligand is added.

# 6. $Ag_2^+(O_2)_n$ clusters

6.1. 
$$Ag_2^+(O_2)$$

The experimental  $\Delta H_T^{\circ}$  and  $\Delta S_T^{\circ}$  values for the association of  $O_2$  with  $Ag_2^+$  are -4.9 kcal/mol and -16.5 cal/(mol K), respectively. The BDE of  $Ag_2^+(O_2)$  was determined by fitting experimental  $\Delta G_T^{\circ}$  vs. T plots (Fig. 3) and found to be 4.5 kcal/mol. Calculations find that the first  $O_2$  ligand binds in a bent configuration to  $Ag_2^+$  in  $C_s$  symmetry (Fig. 4). The calculated (DFT) binding energy  $(D_0)$  of  $Ag_2^+(O_2)$  is 3.78 kcal/mol. As with the  $Ag^+(O_2)_n$  clusters, theory

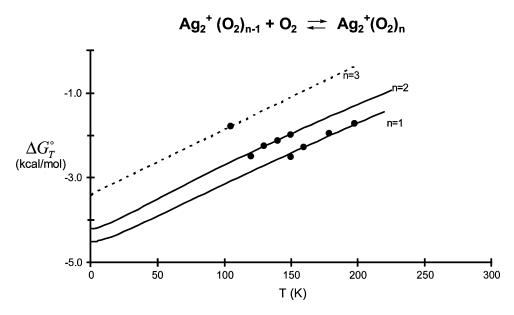


Fig. 3. Plot of experimental  $\Delta G_T^{\circ}$  vs. temperature for the association reactions  $\mathrm{Ag_2}^+(\mathrm{O_2})_{n-1} + \mathrm{O_2} \rightleftarrows \mathrm{Ag_2}^+(\mathrm{O_2})_n$ . Lines are statistical mechanical fits to the data, which yield values of  $\Delta H_0^{\circ}$  at  $T=0\,\mathrm{K}$ .

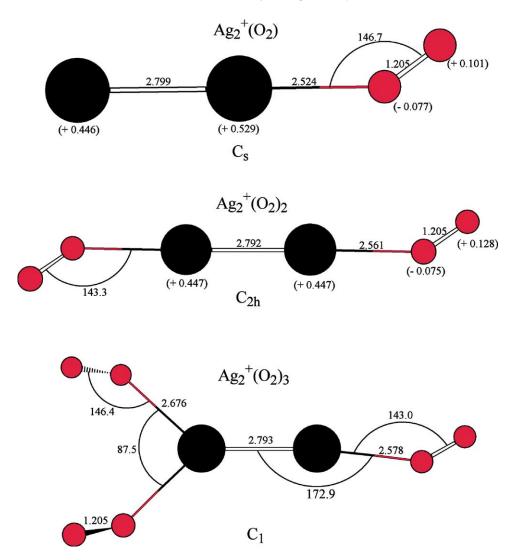


Fig. 4. Theoretical geometries of the  $Ag_2^+(O_2)_n$  clusters calculated at the DFT B3-LYP level. All distances are in angstroms and all angles are in degrees. Partial atomic charges are shown in parentheses. The *z*-axis is taken as the  $Ag_2^+-O_2$  bonding axis.

continues to agree well with experiment. Theoretical vibrational frequencies for  $Ag_2^+(O_2)$  are listed in Table 4. The calculated  $Ag_2^+-O_2$  bond distance is 2.524 Å with an associated O–O bond distance of 1.205 Å. The  $Ag_2^+-O$ –O bond angle is 146.7°.

Bonding in  $Ag_2^+(O_2)$  mimics aspects of the bonding in both the  $Ag^+(O_2)$  and  $Cu_2^+(H_2)$  clusters [12]. The main bonding interactions in  $Ag_2^+(O_2)$  remain largely unchanged from the momomer system. The  $O_2$  ligand adds to  $Ag_2^+$  in a "bent-triatomic" con-

formation indicating the presence of a weak covalent bond formed between  $Ag_2^+$  and  $O_2$  via  $\pi^*(2p_{x,y})$  donation from  $O_2$  to the  $\sigma(5s)$  orbital of  $Ag_2^+$ . This is nearly identical to the bonding interaction in  $Ag^+(O_2)$ . As with  $Ag^+(O_2)$ , a charge-induced dipole moment causes  $O_2$  electron density to be polarized toward  $Ag_2^+$ . The charges on the various atoms are shown in Fig. 4. Furthermore, electron density polarized into the  $\sigma^*(2p_z)$  orbital of  $O_2$  again plays a role in the bonding of the cluster by interacting electrostaticaly

with the  $Ag_2^+$  ion. Here again, NBO population analysis indicates that the amount of electron density in the  $\sigma^*(2p_z)$  orbital is essentially the same as that calculated for the  $Ag^+(O_2)_n$  clusters.

Although  $Ag_2^+(O_2)$  and  $Ag^+(O_2)$  share similar bonding traits, some differences between the two clusters do exist and are similar to the differences found between the Cu<sub>2</sub><sup>+</sup>(H<sub>2</sub>) and Cu<sup>+</sup>(H<sub>2</sub>) clusters. In the  $Ag_2^+(O_2)$  case we find (1) reduced BDEs when compared to that of the analogous momomer cluster (4.5–6.9 kcal/mol), (2) increased transition metal core ion-ligand bond distances and angles, and (3) O-O bond distances closer to those of free O<sub>2</sub>. All of these points can be attributed to a reduction of  $\pi^*(2p_{x,y})$  donation into the  $\sigma(5s)$  orbital of  $Ag_2^+$ . As with  $Cu_2^+$ , this reduction is caused by the single electron occupation of the  $\sigma$  orbital that forms the bond between  $Ag(4d^{10} 5s^1)$  and  $Ag^+(4d^{10} 5s^0)$ . The presence of this electron density in the  $\sigma(5s)$  orbital of  $Ag_2^+$  increases on-axis Pauli repulsion and serves to destabilize the  $Ag_2^+$ – $O_2$  bond when compared to  $Ag^+$ ( $O_2$ ). Calculations show that the  $\sigma(5s)$  electron density of Ag<sub>2</sub><sup>+</sup> is polarized away from the O<sub>2</sub> ligand. This is analogous to what was found in the singly occupied  $\sigma(4s)$  orbital of  $Cu_2^+$ . The cost of polarizing electron density away from the O2 ligand as well as increased on-axis Pauli repulsion and reduced donation to Ag<sub>2</sub><sup>+</sup> gives rise to the reduced bond strength in  $Ag_2^+(O_2)$ .

# 6.2. $Ag_2^+(O_2)_2$ and $Ag_2^+(O_2)_3$

The experimental  $\Delta H_T^{\circ}$  and  $\Delta S_T^{\circ}$  values for the formation of  $Ag_2^+(O_2)_2$  are -4.5 kcal/mol and -16.0 cal/(mol K), respectively. The BDE of  $Ag_2^+(O_2)_2$  was determined by the usual analysis of experimental  $\Delta G_T^{\circ}$  vs. T curves and was found to be 4.2 kcal/mol. The calculated (DFT) binding energy  $(D_0)$  of  $Ag_2^+(O_2)_2$  is 3.16 kcal/mol. Again, reasonable agreement between experiment and theory was obtained. The second  $O_2$  ligand adds opposite the first in  $C_{2h}$  symmetry (Fig. 4). The calculated  $Ag^+-O$  bond distance is 2.561 Å with an associated O-O bond length of 1.205 Å. The  $Ag_2^+-O-O$  bond angle is approximately 143.3°. Theoretical vibrational fre-

quencies for  $Ag_2^+(O_2)_2$  are given in Table 4. As with  $Ag^+(O_2)_2$ , alternative minimum energy conformers exist for  $Ag_2^+(O_2)_2$ , which are degenerate within the accuracy of the calculation. The first is in  $C_{2v}$  symmetry (cis) and the second is in  $C_2$  symmetry, with one of the  $C_2$  ligands rotated  $C_2$ 0° out of plane with respect to the other. A transition state structure was calculated in which one  $C_2$ 1 ligand was rotated approximately  $C_2$ 1 out of plane. The barrier height was found to be approximately  $C_2$ 2 out of plane. The system (as in the  $C_2$ 3 cluster).

The bonding interactions of  $Ag_2^+(O_2)_2$  are essentially unchanged from  $Ag_2^+(O_2)$ , dominated by  $\pi^*(2p_{x,y})$  donation from the  $O_2$  ligands to the  $\sigma(5s)$  orbital of  $Ag_2^+$  and supplemented by an electrostatic interaction of the  $\sigma^*(2p_z)$  orbital of the  $O_2$  ligands with  $Ag_2^+$ . As with the other clusters discussed in this work, the core ion charge causes the electron density of the  $O_2$  ligands to be polarized toward the  $Ag_2^+$  core.

Although the bonding of  $Ag_2^+(O_2)_2$  is quite similar to Ag<sub>2</sub><sup>+</sup>(O<sub>2</sub>), the measured BDE of the former cluster is slightly reduced with respect to the latter. This result is unlike the Ag+ clusters, where the second O<sub>2</sub> ligand binds more strongly than the first because the energy cost of  $4d_{x^2-y^2}/5s$  orbital hybridization of Ag<sup>+</sup> is paid upon the first O<sub>2</sub> addition. This increase in BDE does not occur in  $Ag_2^+(O_2)_2$  due to the single occupation of the  $\sigma(5s)$  orbital of  $Ag_2^+$ . Here, much like the singly occupied  $\sigma(4s)$  orbital of  $Cu_2^+(H_2)_2$ , repulsive  $\sigma(5s)$  electron density is initially polarized away from the first O<sub>2</sub> ligand. Consequentially, addition of the second ligand must now occur in an area of relatively high electron density. In order to reduce the amount of on-axis repulsion experienced by the second ligand,  $\sigma(5s)$  electron density is "repolarized" to near its original distribution in the bare  $Ag_2^+$  core ion. The effect of this process is a decrease in the overall bond strength of  $Ag_2^+(O_2)_2$ .

A single data point for  $Ag_2^+(O_2)_3$  formation was taken at 120 K. This data point was matched with the entropy of the  $Ag_2^+$  second cluster in order to estimate a BDE of 3.5 kcal/mol for  $Ag_2^+(O_2)_3$ . The DFT

optimized structure for  $Ag_2^+(O_2)_3$  is shown in Fig. 4. The theoretical binding energy  $(D_0)$  for  $Ag_2^+(O_2)_3$  is 1.76 kcal/mol, in reasonable agreement with the estimated experimental value. The theoretical structure of  $Ag_2^+(O_2)_3$  (Fig. 4) shows that the addition of the third  $O_2$  ligand is to one of the Ag atoms in  $Ag_2^+$ , causing the previously bound ligand to shift approximately 87.5° from the newly bound  $O_2$ . Several factors, including reduced electron donation to  $Ag_2^+$ , increased  $\sigma(5s)$  repulsion, and ligand–ligand repulsion combine to cause the reduction in bond strength of  $Ag_2^+(O_2)_3$ .

#### 7. Conclusions

- 1. Bond dissociation energies and association entropies were determined for  $Ag^+(O_2)_{1-4}$  and  $Ag_2^+(O_2)_{1-3}$ . The  $Ag^+$  BDEs are (in order of cluster size) 6.9, 7.4, 5.5, and  $\sim$ 4.8 kcal/mol. The  $Ag_2^+$  BDEs are (in order of cluster size) 4.5, 4.2, and  $\sim$ 3.5 kcal/mol.
- 2. Density functional theory calculations (B3-LYP parameterization) were done on all the ions to obtain theoretical BDEs, geometries, rotational constants, and vibrational frequencies. Agreement between the theoretical and experimental BDEs is in all cases good, with experimental trends being reproduced by theory although the theoretical BDEs are systematically too small by 0.5–1.0 kcal/mol.
- 3. Bonding in the clusters consists mainly of electron donation to  $Ag^+$  and  $Ag_2^+$  from the  $O_2$   $\pi^*(2p_{x,y})$  orbital, combined with a minor electrostatic interaction between the  $\sigma^*(2p_z)$  orbital of  $O_2$  with the  $Ag^+$  and  $Ag_2^+$  ions, respectively. In all cases, charge induced dipole moments on the  $O_2$  ligands were found to play a role in the bonding of the clusters.
- 4. The bonding interactions in the  $Ag^+(O_2)_n$  and  $Ag_2^+(O_2)_n$  cluster ions resembled those in the  $Cu^+(H_2)_n$  and the  $Cu_2^+(H_2)_n$  systems, respectively. This is not unexpected since the valence shell electron configurations of the  $Ag^+(4d^{10})$  and  $Ag_2^+(4d^{20}\ \sigma(5s)^1)$  ions are directly analogous to the  $Cu^+(3d^{10})$  and  $Cu_2^+(3d^{20}\ \sigma(4s)^1)$  ions.

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